

Baselines and  
Oscillation  
Nodes

Mary Bishai

Nodes and  
Asymmetries

Neutrino  
Fluxes

Event Rates

Rate  
Asymmetries

LBNE/LBNO  
comparisons

# Baselines and Oscillation Nodes

## LBPWG, 08/08/2013

Mary Bishai

August 20, 2014

# Outline

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## 1 Nodes and Asymmetries

## 2 Neutrino Fluxes

## 3 Event Rates

## 4 Rate Asymmetries

## 5 LBNE/LBNO comparisons

# CP Asymmetry vs $E_\nu$ and $\delta_{cp}$

Baselines and  
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Nodes and  
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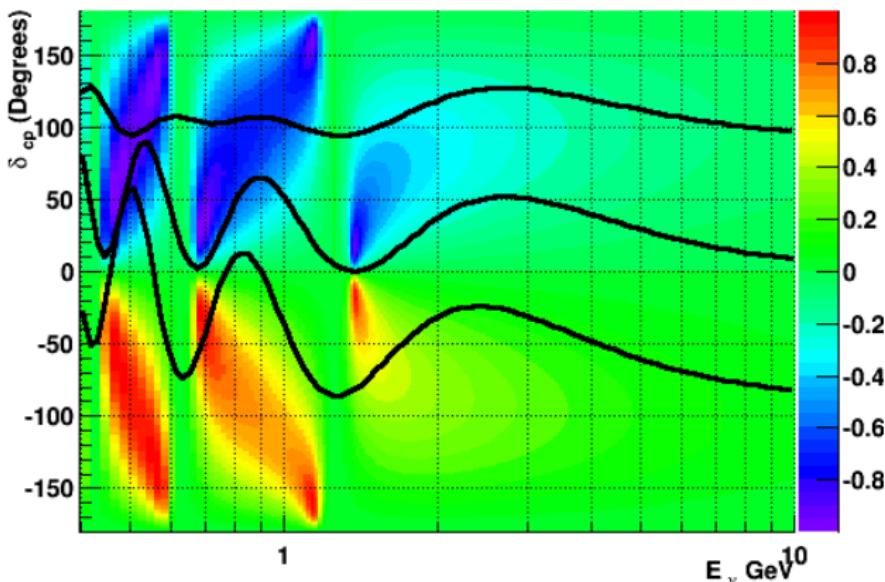
Neutrino  
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Asymmetry at 1300km (Total), vacuum



Asymmetries are larger near minima

BUT, events appear at the maxima!

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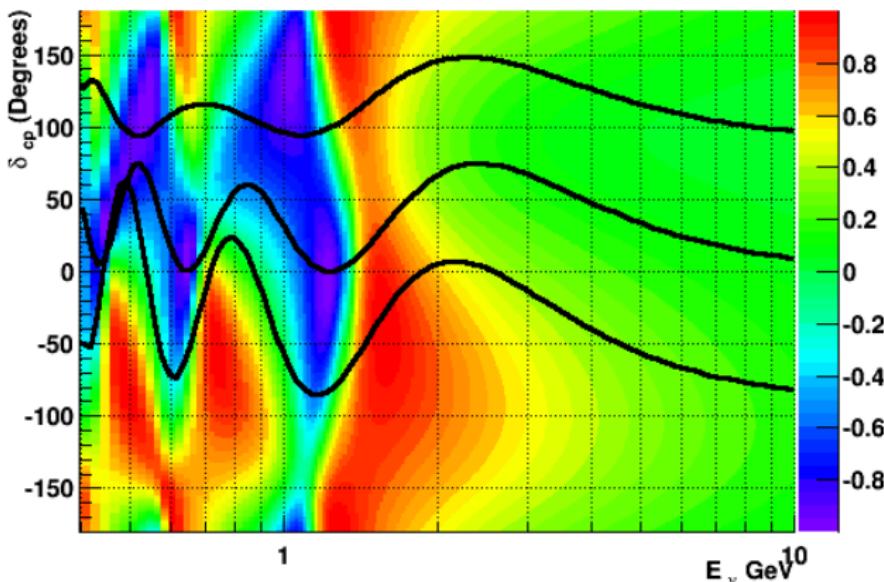
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Asymmetry at 1300km (Total), NH



Asymmetries are larger near **minima**

BUT, events appear at the **maxima!**

# CP Asymmetry vs $E_\nu$ and $\delta_{cp}$

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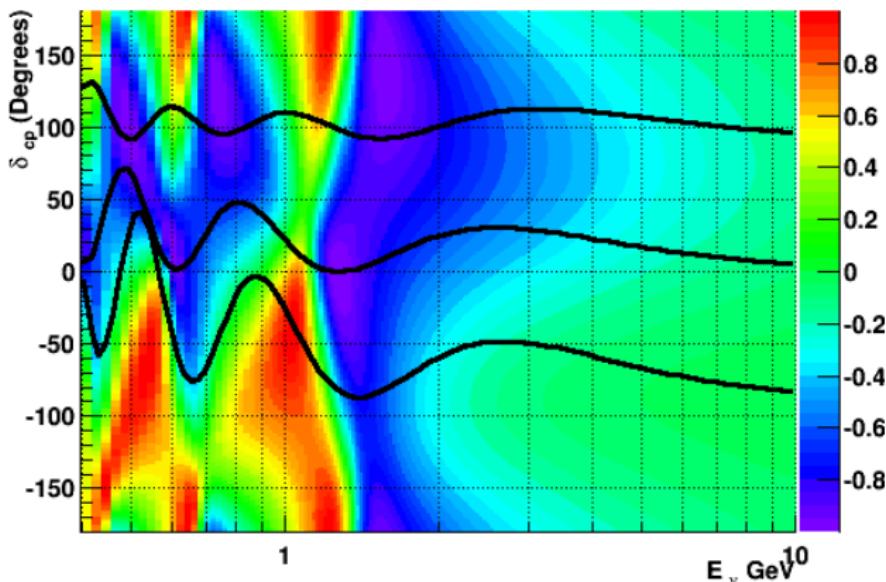
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Asymmetry at 1300km (Total), IH



Asymmetries are larger near **minima**

BUT, events appear at the **maxima!**

# Matter and CP Asymmetries at Maxima

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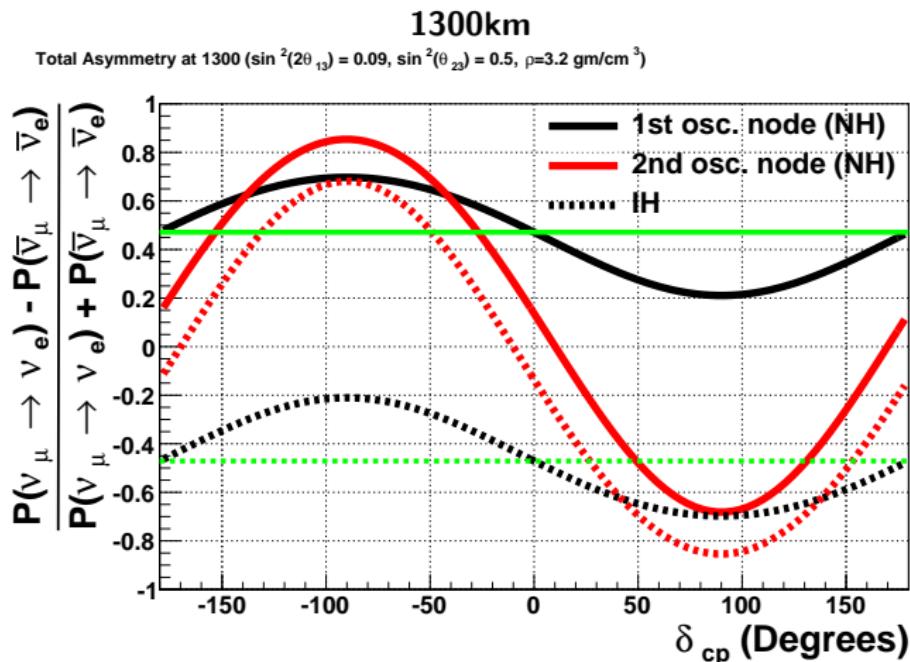
Nodes and  
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$$\begin{aligned} A_{\text{matter}}^1 &= 0.5, \quad A_{\text{CP}}^1 = 0.2 \\ A_{\text{matter}}^2 &= 0.1, \quad A_{\text{CP}}^2 = 0.7 \end{aligned}$$

# Matter and CP Asymmetries at Maxima

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Oscillation  
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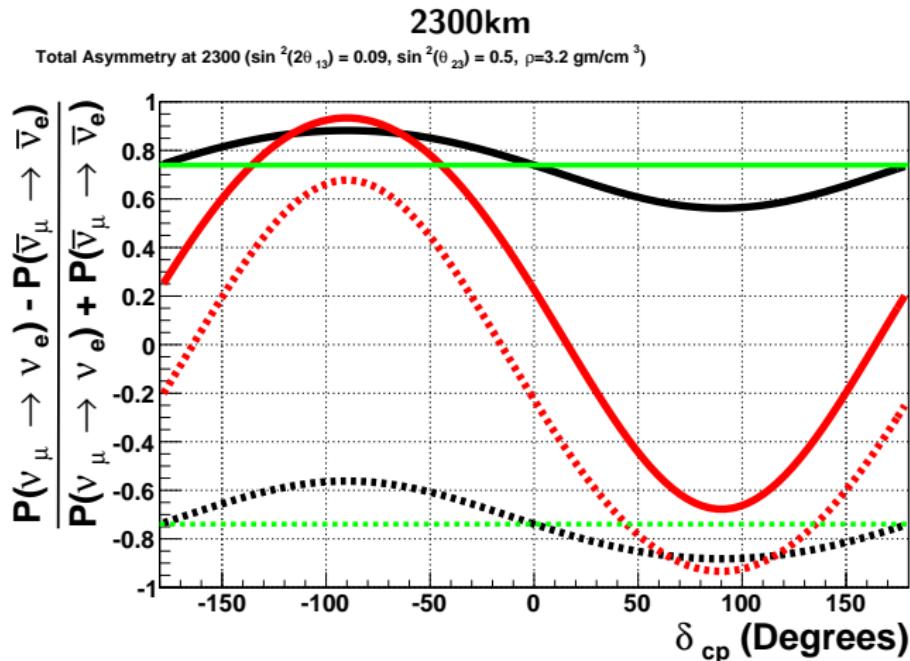
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$$\begin{aligned}\mathcal{A}_{\text{matter}}^1 &= 0.75, \quad \mathcal{A}_{\text{CP}}^1 = 0.2 \\ \mathcal{A}_{\text{matter}}^2 &= 0.2, \quad \mathcal{A}_{\text{CP}}^2 = 0.7\end{aligned}$$

# Osc. vs L/E

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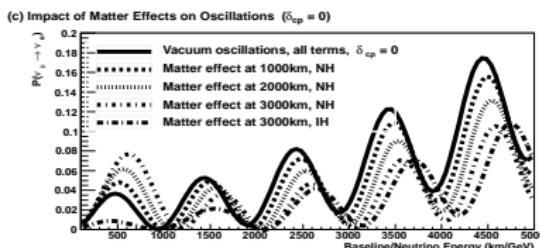
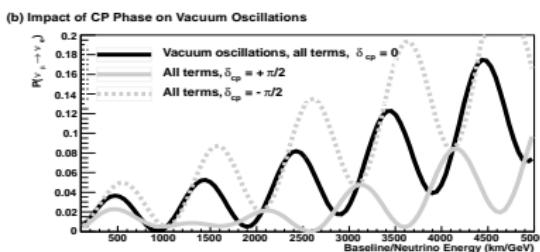
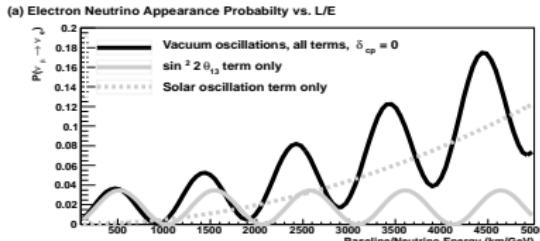
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1st oscillation node is from  
 $L/E \sim 100\text{km}/\text{GeV}$  to  
 $1000\text{ km}/\text{GeV}$

2nd oscillation node is from  
 $L/E \sim 1000\text{km}/\text{GeV}$  to  
 $2000\text{ km}/\text{GeV}$

Assuming flat flux and  
 $\sigma_\nu^2 / \sigma_\nu^1 = 0.4$ ,  
integrated event rates in  
vacuum over 1st and 2nd  
oscillation nodes are:

$$\begin{aligned} \frac{R^2}{R^1} &= \frac{(1/1000 - 1/2000)}{(1/100 - 1/1000)} \\ &\times \frac{0.05}{0.035} \\ &\times 0.4 \\ &= 3\% \end{aligned}$$

# Neutrino fluxes with perfect focusing

Baselines and  
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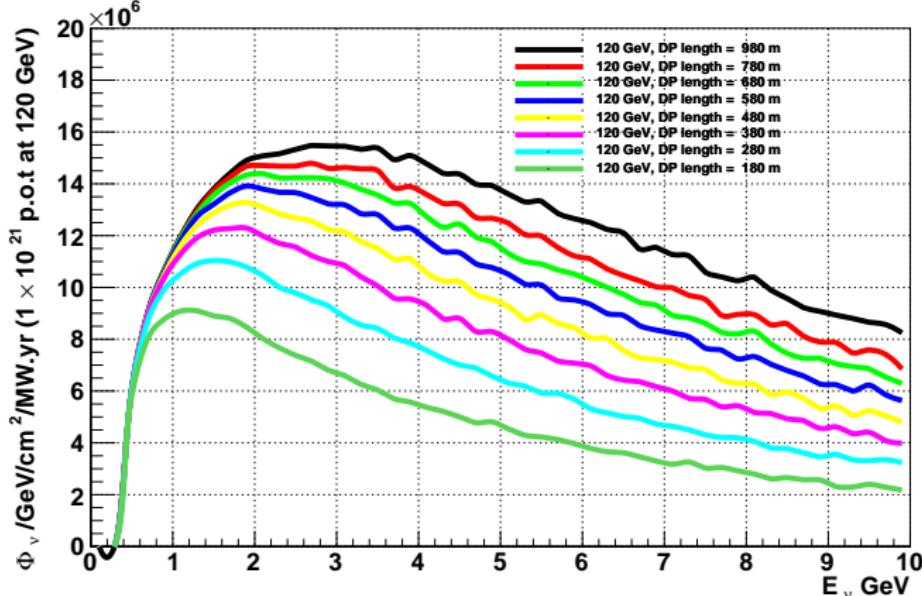
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## 120 GeV, decay channel lengths from 200m to 1km

Flux at 1000km, perfect focusing, different decay pipe lengths



# Neutrino fluxes with perfect focusing

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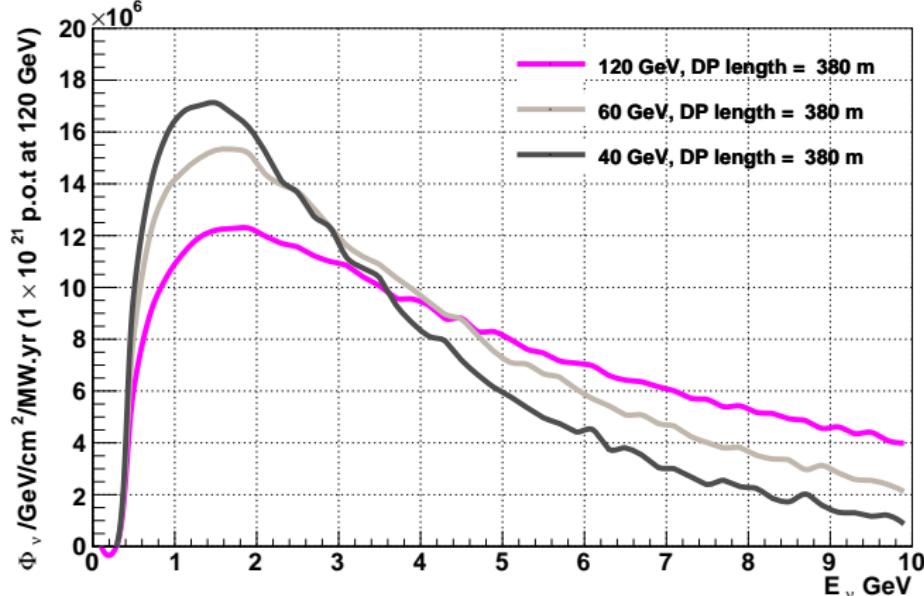
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40 to 120 GeV, decay channel length = 400m

Flux at 1000km, perfect focusing, beam energies



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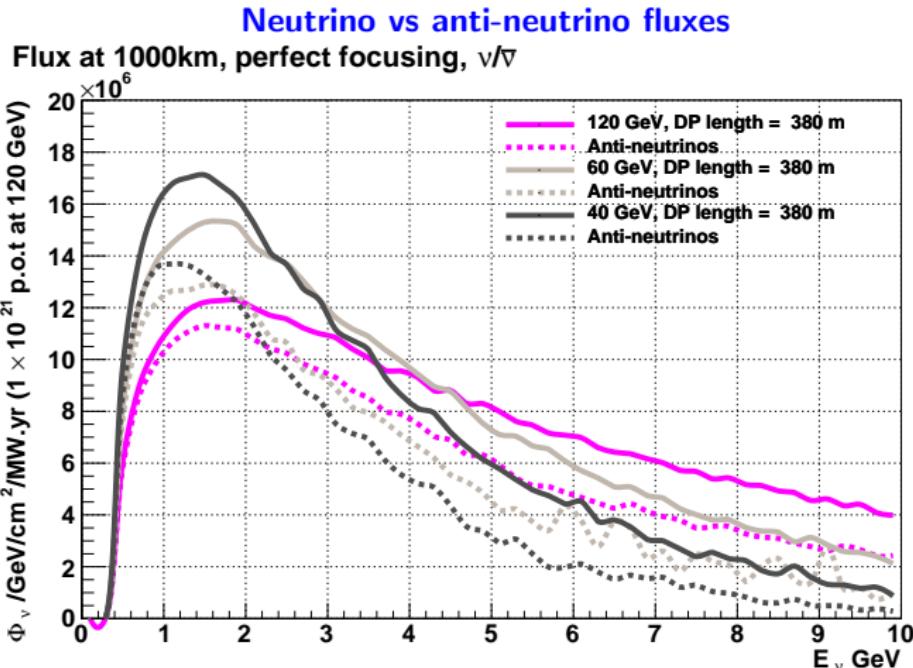
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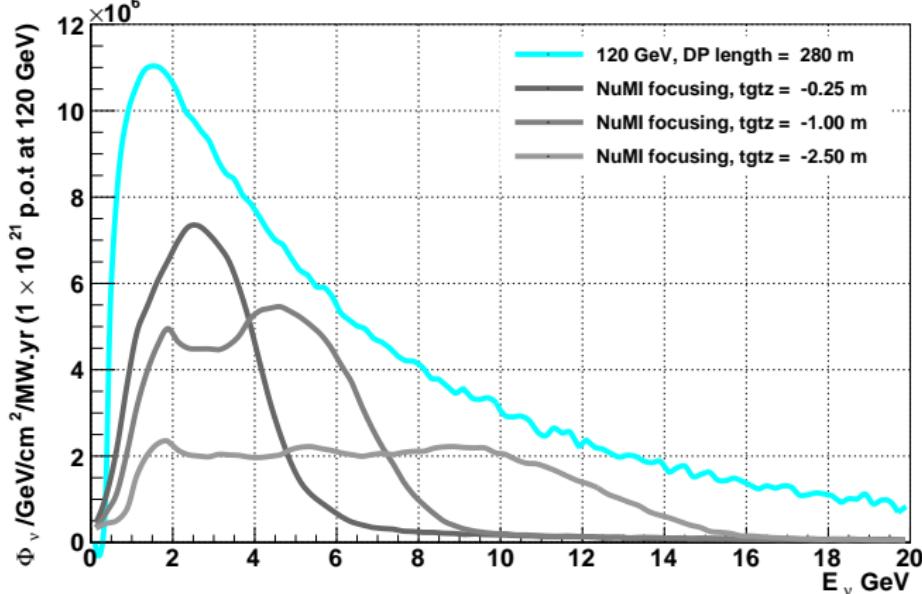
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## Variable NuMI Focusing

Flux at 1000km, NuMI focusing, 230kA, H1-H2 = 6.6m



# Event Rates vs. Baseline

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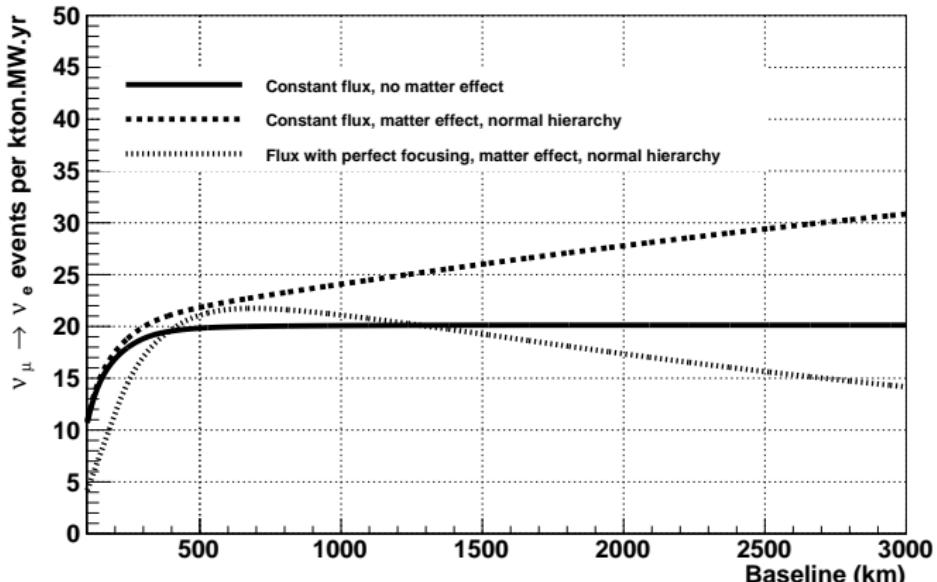
$$\mathcal{R} = \int \Phi_{\text{perfect}}^{\nu_\mu}(E_\nu) \times \sigma(E_\nu) \times P(\nu_\mu \rightarrow \nu_e) dE_\nu$$

$(\sin^2 2\theta_{13} = 0.09, \sin^2 \theta_{23} = 0.5, \delta_{cp} = 0, |\Delta m_{31}^2| = 2.4 \times 10^{-3})$

Flux: 120 GeV, perfect focusing,  $\sim 400$ m decay channel, on-axis

## Normal Hierarchy

### Appearance rates versus baseline



# Event Rates vs. Baseline

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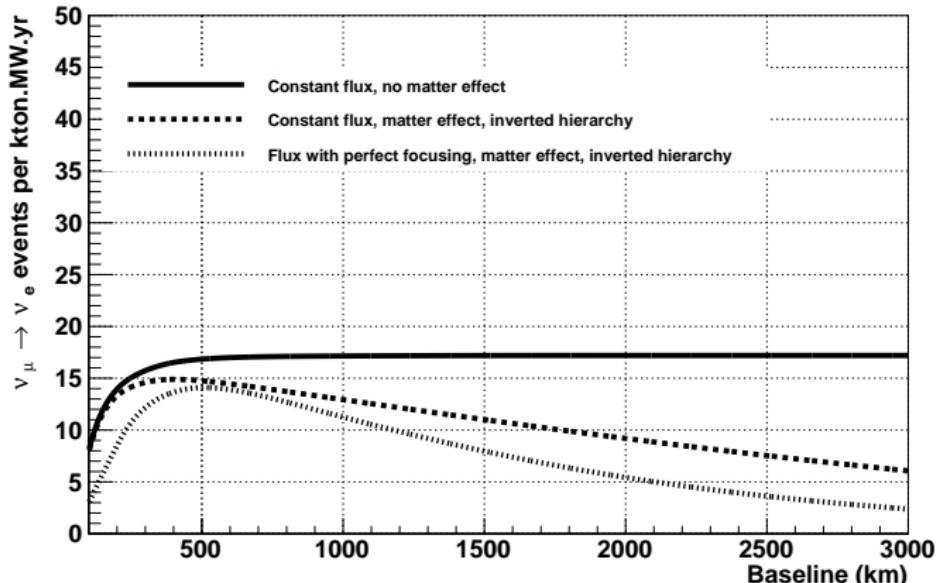
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## Inverted Hierarchy

### Appearance rates versus baseline



# Event Rates vs. Baseline at 1<sup>st</sup> and 2<sup>nd</sup> Osc. Nodes

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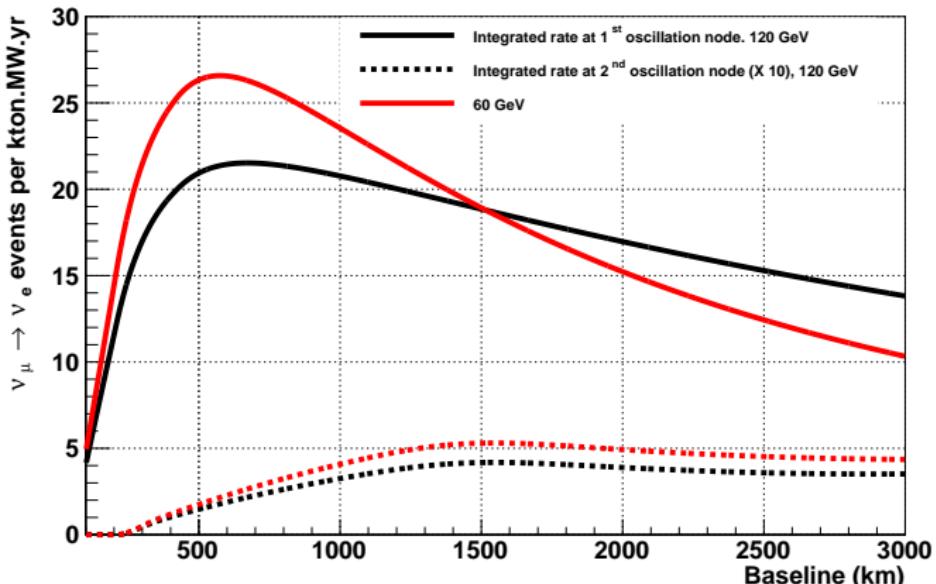
LBNE/LBNO  
comparisons

$$1^{\text{st}} \text{ osc. node from } E_1 = 1.267 |\Delta m_{31}^2| L / \pi \text{ to } 10 \times E_1$$

$$2^{\text{nd}} \text{ osc node from } E_2 = 1.267 |\Delta m_{31}^2| L / (2\pi) \text{ to } E_1$$

## Normal Hierarchy

$\nu_\mu \rightarrow \nu_e$  appearance rates versus baseline



# Event Rates vs. Baseline at 1<sup>st</sup> and 2<sup>nd</sup> Osc. Nodes

Baselines and  
Oscillation  
Nodes

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Event Rates

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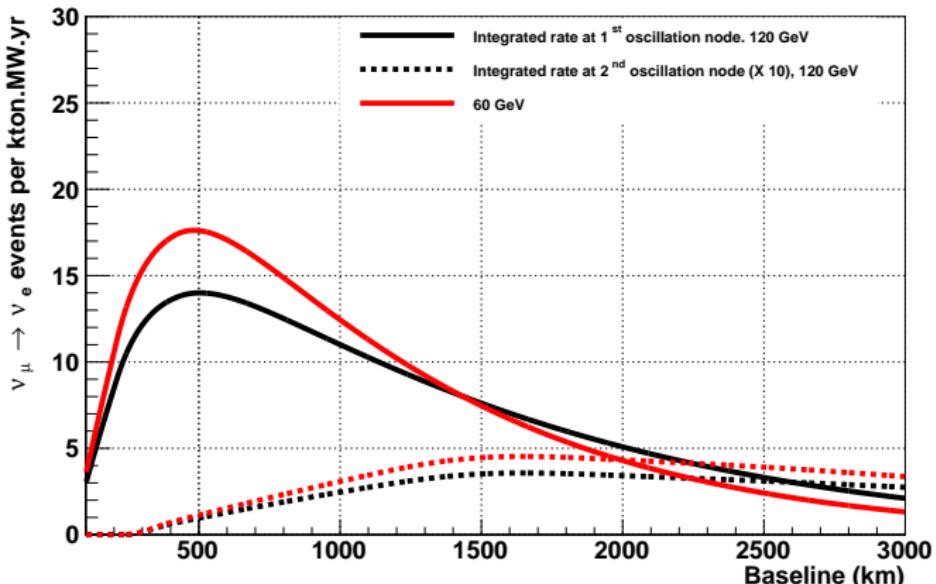
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## Inverted Hierarchy

$\nu_\mu \rightarrow \nu_e$  appearance rates versus baseline



# Event Rates vs. Baseline at 1<sup>st</sup> and 2<sup>nd</sup> Osc. Nodes

1<sup>st</sup> osc. node from  $E_1 = 1.267|\Delta m_{31}^2|L/\pi$  to  $10 \times E_1$

2<sup>nd</sup> osc node from  $E_2 = 1.267|\Delta m_{31}^2|L/(2\pi)$  to  $E_1$

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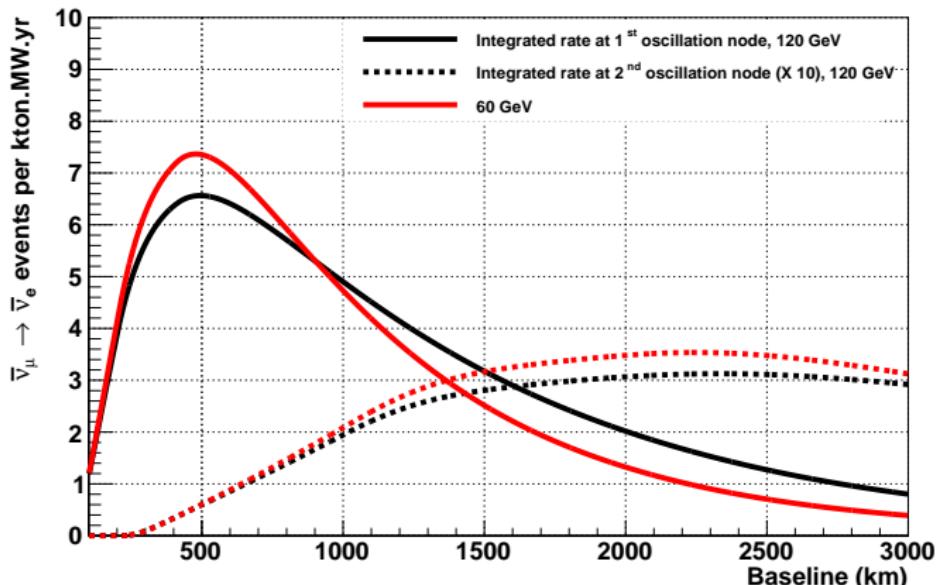
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## Normal Hierarchy

$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  appearance rates versus baseline



# Event Rates vs. Baseline at 1<sup>st</sup> and 2<sup>nd</sup> Osc. Nodes

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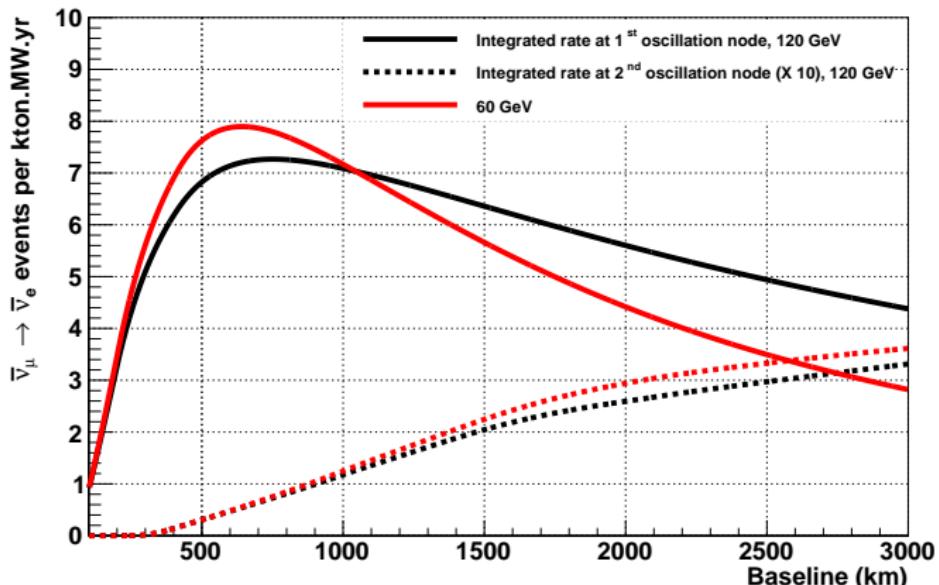
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$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  appearance rates versus baseline



# Integrated Rate Asymmetries w/ Perfect Focusing

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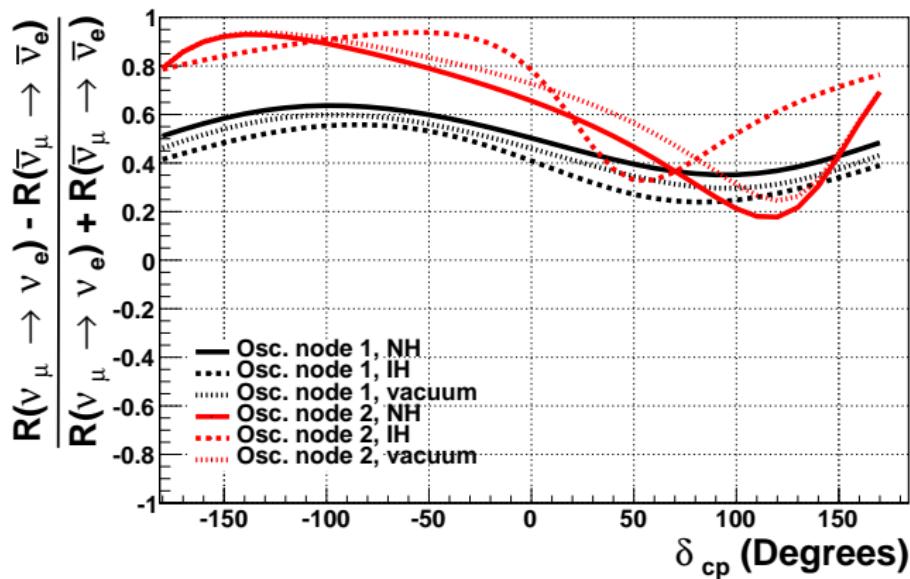
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300 km

Integrated Rate Asymmetry at 300 km ( $\sin^2(2\theta_{13}) = 0.09, \sin^2(\theta_{23}) = 0.50, \rho = 2.8 \text{ gm/cm}^3$ )



# Integrated Rate Asymmetries w/ Perfect Focusing

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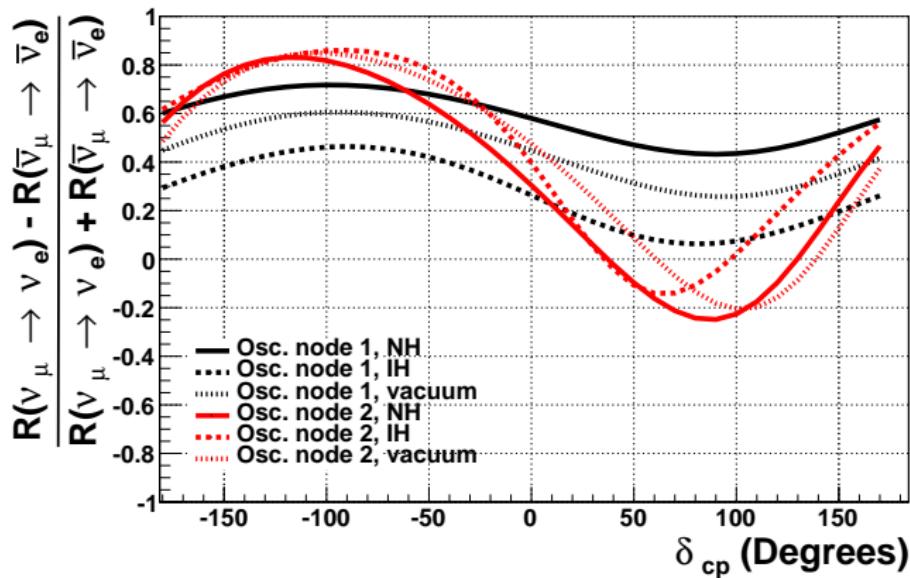
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810 km

Integrated Rate Asymmetry at 810 km ( $\sin^2(2\theta_{13}) = 0.09, \sin^2(\theta_{23}) = 0.50, \rho = 2.8 \text{ gm/cm}^3$ )



# Integrated Rate Asymmetries w/ Perfect Focusing

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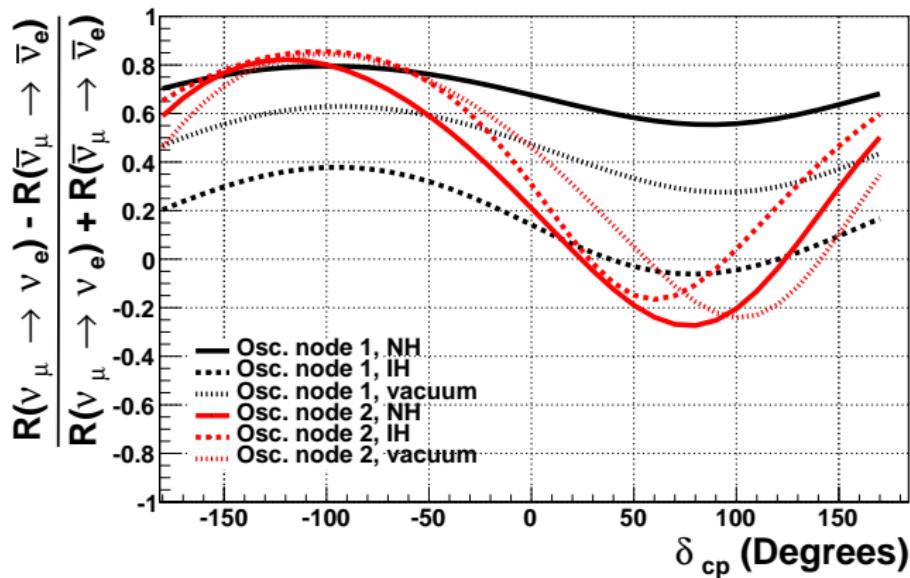
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1300 km

Integrated Rate Asymmetry at 1300 km ( $\sin^2(2\theta_{13}) = 0.09, \sin^2(\theta_{23}) = 0.50, \rho = 2.8 \text{ gm/cm}^3$ )



# Integrated Rate Asymmetries w/ Perfect Focusing

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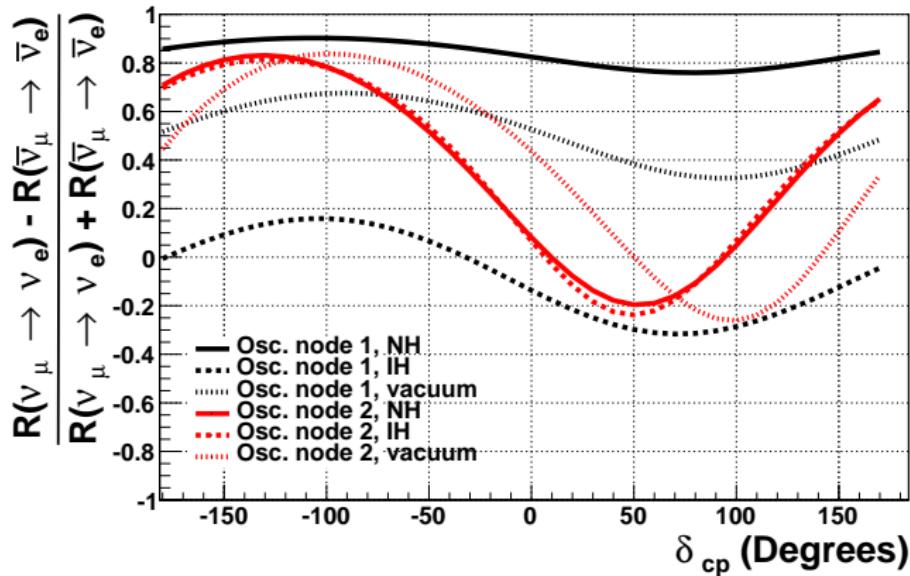
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2300 km

Integrated Rate Asymmetry at 2300 km ( $\sin^2(2\theta_{13}) = 0.09, \sin^2(\theta_{23}) = 0.50, \rho = 2.8 \text{ gm/cm}^3$ )



# LBNO/LBNO fluxes

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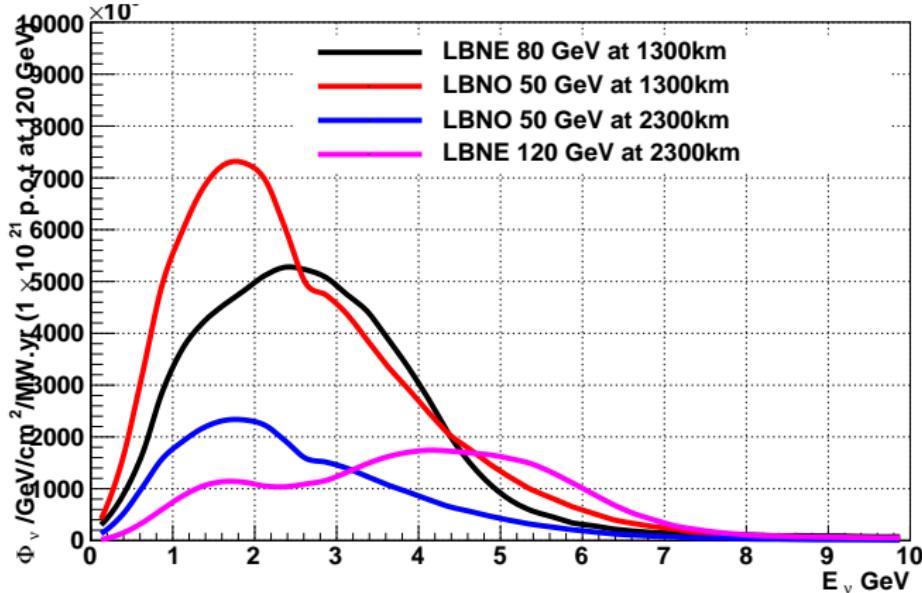
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## Forward horn current

### $\nu_\mu$ fluxes at 1300 and 2300km



# LBNO/LBNO fluxes

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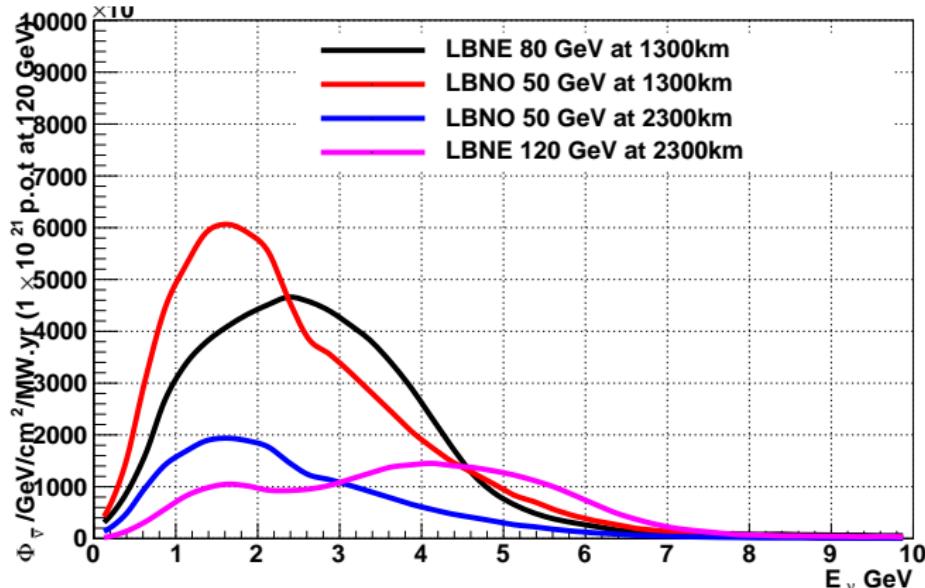
Event Rates

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## Reverse horn current

### $\nabla_\mu$ fluxes at 1300 and 2300km



# Appearance Spectra (no detector effects) NH

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Baselines and  
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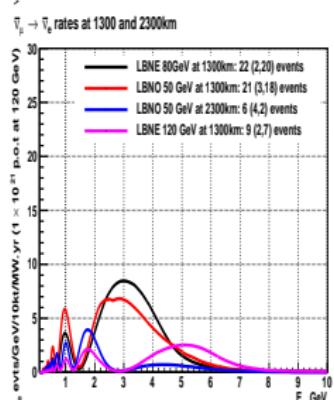
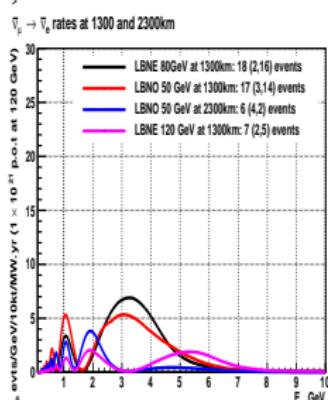
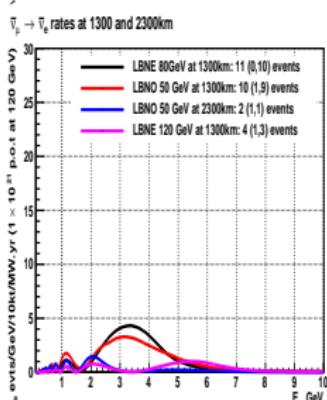
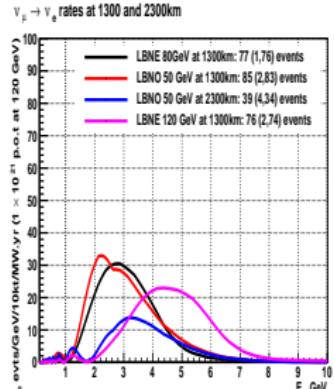
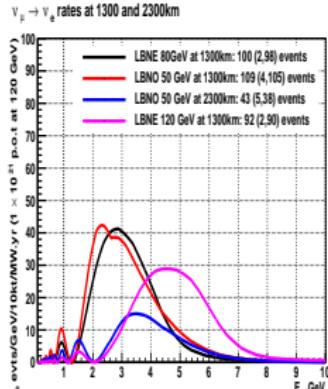
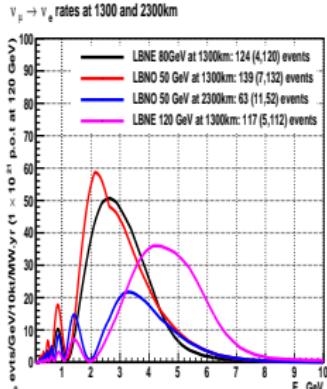
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# Appearance Spectra (no detector effects) IH

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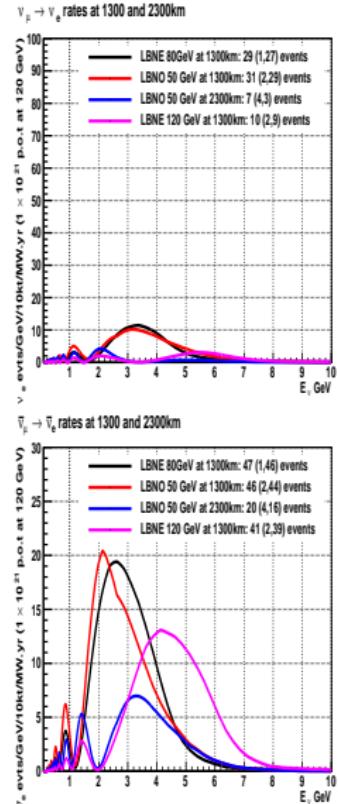
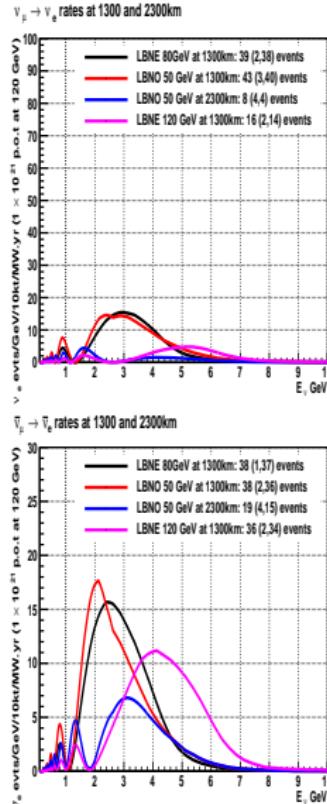
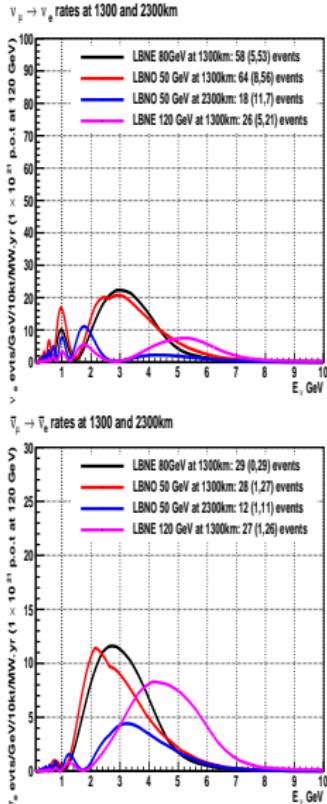
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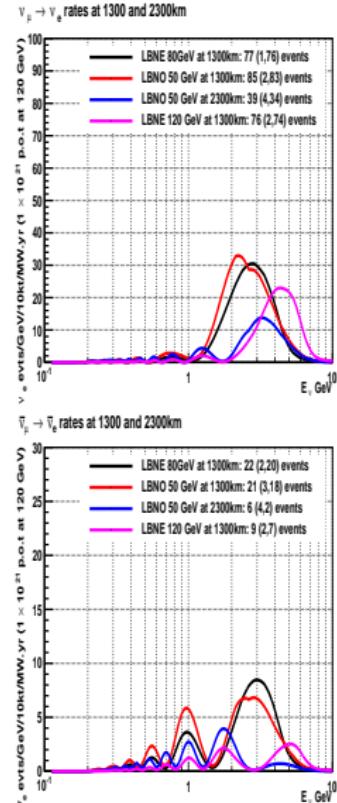
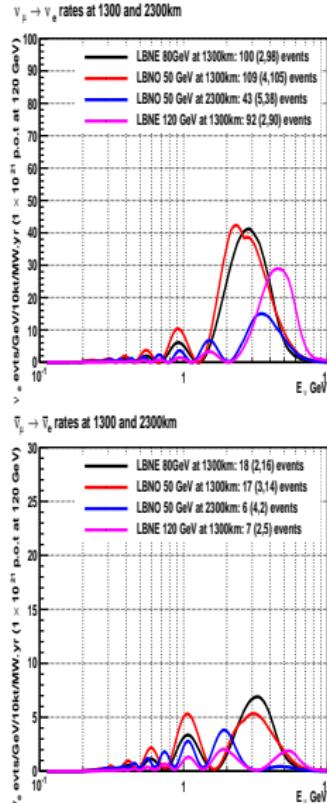
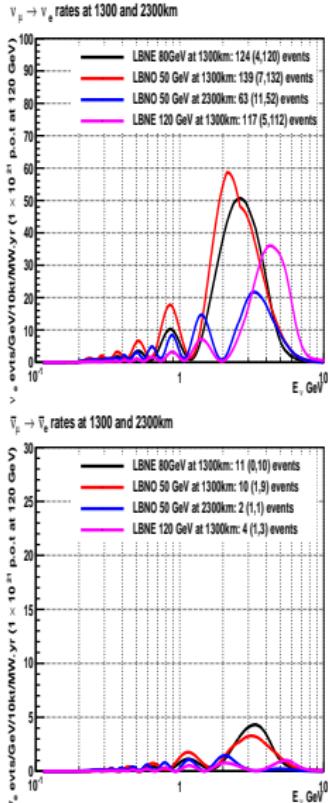
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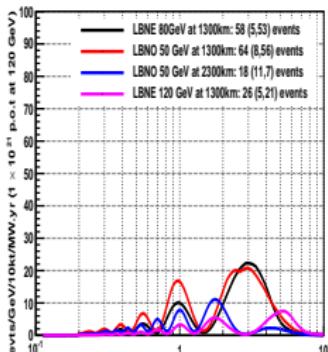
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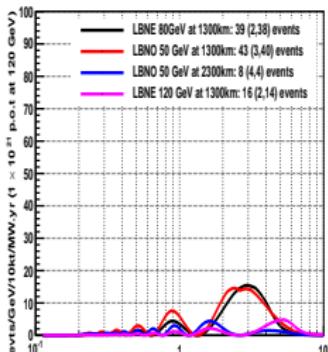
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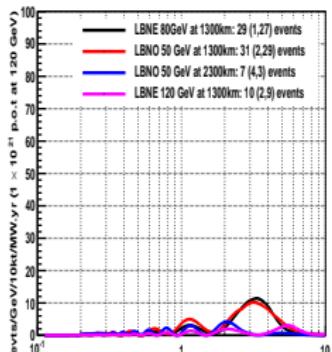
$\nu_\mu \rightarrow \nu_e$  rates at 1300 and 2300km



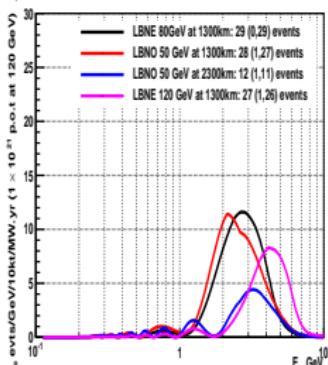
$\nu_\mu \rightarrow \nu_e$  rates at 1300 and 2300km



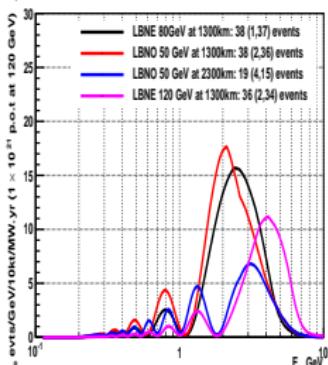
$\nu_\mu \rightarrow \nu_e$  rates at 1300 and 2300km



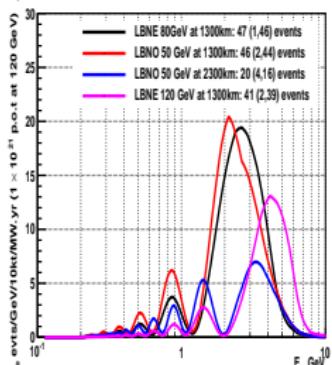
$\nu_\mu \rightarrow \bar{\nu}_e$  rates at 1300 and 2300km



$\nu_\mu \rightarrow \bar{\nu}_e$  rates at 1300 and 2300km



$\nu_\mu \rightarrow \bar{\nu}_e$  rates at 1300 and 2300km



# Appearance Rates vs. $\delta_{\text{cp}}$ (no detector effects)

## 1<sup>st</sup> Osc. Node      $\geq$ 2<sup>nd</sup> Osc. Node

Baselines and  
Oscillation  
Nodes

Mary Bishai

Nodes and  
Asymmetries

Neutrino  
Fluxes

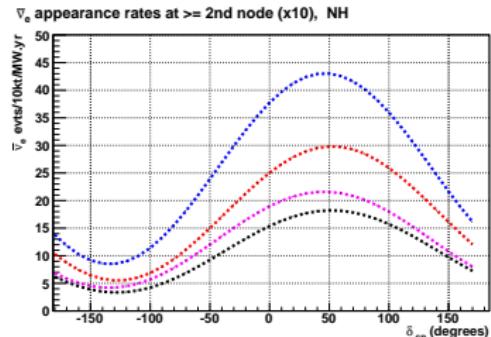
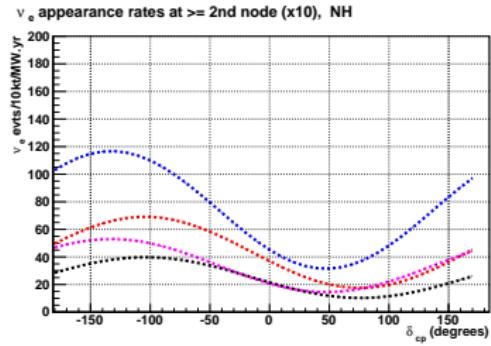
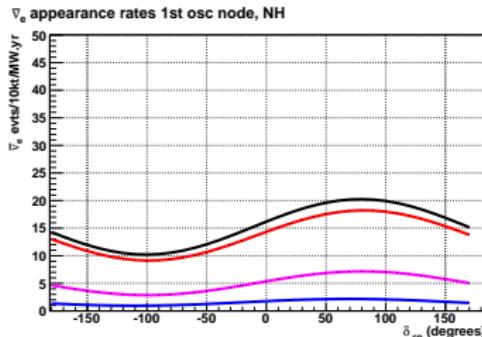
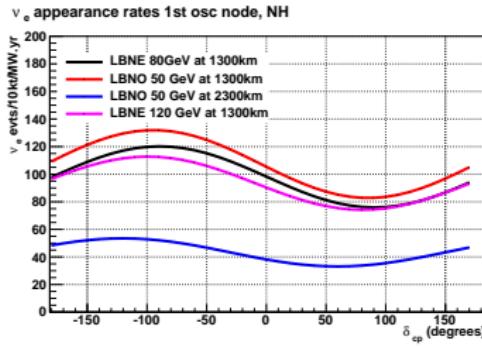
Event Rates

Rate  
Asymmetries

LBNE/LBNO  
comparisons

$$(\sin^2 2\theta_{13} = 0.09, \sin^2 \theta_{23} = 0.45, |\Delta m_{31}^2| = 2.5 \times 10^{-3}, \rho = 3.2 \text{ gm/cm}^3)$$

**Normal Hierarchy**



# Appearance Rates vs. $\delta_{\text{cp}}$ (no detector effects)

## 1<sup>st</sup> Osc. Node      $\geq$ 2<sup>nd</sup> Osc. Node

Baselines and  
Oscillation  
Nodes

Mary Bishai

Nodes and  
Asymmetries

Neutrino  
Fluxes

Event Rates

Rate  
Asymmetries

LBNE/LBNO  
comparisons

$$(\sin^2 2\theta_{13} = 0.09, \sin^2 \theta_{23} = 0.45, |\Delta m_{31}^2| = 2.5 \times 10^{-3}, \rho = 3.2 \text{ gm/cm}^3)$$

**Inverted Hierarchy**

